

First order approximation of stochastic models

Shanghai Dynare Workshop

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Outline

- 1 Presentation of the problem
- 2 The solution function
- 3 The steady state
- 4 First order approximation
- 5 Example
- 6 Dating variables in Dynare
- 7 The Dynare preprocessor

General problem

$$E_t \{f(y_{t+1}, y_t, y_{t-1}, u_t)\} = 0$$

$$E(u_t) = 0$$

$$E(u_t u_t') = \Sigma_u$$

$$E(u_t u_\tau') = 0 \quad t \neq \tau$$

y : vector of endogenous variables

u : vector of exogenous stochastic shocks

Computation of first order approximation

- Perturbation approach: recovering a Taylor expansion of the solution function from a Taylor expansion of the original model.
- A first order approximation is nothing else than a standard solution thru linearization.
- A first order approximation in terms of the logarithm of the variables provides standard log-linearization.

Timing assumptions

$$E_t \{f(y_{t+1}, y_t, y_{t-1}, u_t)\} = 0$$

- shocks u_t are observed at the beginning of period t ,
- decisions affecting the current value of the variables y_t , are function of
 - ▶ the previous state of the system, y_{t-1} ,
 - ▶ the shocks u_t .

The stochastic scale variable

$$E_t \{f(y_{t+1}, y_t, y_{t-1}, u_t)\} = 0$$

- At period t , the only unknown stochastic variable is y_{t+1} , and, implicitly, u_{t+1} .
- We introduce the *stochastic scale variable*, σ and the auxiliary random variable, ϵ_t , such that

$$u_{t+1} = \sigma \epsilon_{t+1}$$

The stochastic scale variable (continued)

$$E(\epsilon_t) = 0 \quad (1)$$

$$E(\epsilon_t \epsilon'_t) = \Sigma_\epsilon \quad (2)$$

$$E(\epsilon_t \epsilon'_\tau) = 0 \quad t \neq \tau \quad (3)$$

and

$$\Sigma_u = \sigma^2 \Sigma_\epsilon$$

$$E_t \{f(y_{t+1}, y_t, y_{t-1}, u_t)\} = 0$$

- The exogenous shocks may appear only at the current period
- There is no deterministic exogenous variables
- Not all variables are necessarily present with a lead and a lag
- Generalization to leads and lags on more than one period: similar to deterministic case, but more complicated for lead variables (because of expectancy operator)

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Solution function

$$y_t = g(y_{t-1}, u_t, \sigma)$$

where σ is the stochastic scale of the model. If $\sigma = 0$, the model is deterministic. For $\sigma > 0$, the model is stochastic.

Under some conditions, the existence of $g()$ function is proven via an implicit function theorem. See H. Jin and K. Judd “Solving Dynamic Stochastic Models” (<http://bucky.stanford.edu/papers/PerturbationMethodRatEx.pdf>)

Solution function (continued)

Then,

$$\begin{aligned}y_{t+1} &= g(y_t, u_{t+1}, \sigma) \\ &= g(g(y_{t-1}, u_t, \sigma), u_{t+1}, \sigma)\end{aligned}$$

Let's:

$$\begin{aligned}F(y_{t-1}, u_t, \epsilon_{t+1}, \sigma) \\ = f(g(g(y_{t-1}, u_t, \sigma), \sigma \epsilon_{t+1}, \sigma), g(y_{t-1}, u_t, \sigma), y_{t-1}, u_t)\end{aligned}$$

So that the problem is redefined as:

$$E_t \{F(y_{t-1}, u_t, \epsilon_{t+1}, \sigma)\} = 0$$

The perturbation approach

- Obtain a Taylor expansion of the unknown solution function in the neighborhood of a problem that we know how to solve.
- The problem that we know how to solve is the deterministic steady state.
- One obtains the Taylor expansion of the solution for the Taylor expansion of the original problem.
- One consider two different perturbations:
 - 1 points in the neighborhood from the steady state,
 - 2 from a deterministic model towards a stochastic one (by increasing σ from a zero value).

The perturbation approach (continued)

- The Taylor approximation is taken with respect to y_{t-1} , u_t and σ , the arguments of the solution function

$$y_t = g(y_{t-1}, u_t, \sigma).$$

- At the deterministic steady state, all derivatives are deterministic as well.

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Steady state

A deterministic steady state, \bar{y} , for the model satisfies

$$f(\bar{y}, \bar{y}, \bar{y}, 0) = 0$$

A model can have several steady states, but only one of them will be used for approximation.

Furthermore,

$$\bar{y} = g(\bar{y}, 0, 0)$$

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First order approximation

Around \bar{y} :

$$\begin{aligned} E_t \left\{ F^{(1)}(y_{t-1}, u_t, \epsilon_{t+1}, \sigma) \right\} &= \\ E_t \left\{ f(\bar{y}, \bar{y}, \bar{y}, 0) + f_{y_+} (g_y (g_y \hat{y} + g_u u + g_\sigma \sigma) + g_u \sigma \epsilon' + g_\sigma \sigma) \right. \\ &\quad \left. + f_{y_0} (g_y \hat{y} + g_u u + g_\sigma \sigma) + f_{y_-} \hat{y} + f_u u \right\} \\ &= 0 \end{aligned}$$

with $\hat{y} = y_{t-1} - \bar{y}$, $u = u_t$, $\epsilon' = \epsilon_{t+1}$, $f_{y_+} = \frac{\partial f}{\partial y_{t+1}}$, $f_{y_0} = \frac{\partial f}{\partial y_t}$, $f_{y_-} = \frac{\partial f}{\partial y_{t-1}}$,
 $f_u = \frac{\partial f}{\partial u_t}$, $g_y = \frac{\partial g}{\partial y_{t-1}}$, $g_u = \frac{\partial g}{\partial u_t}$, $g_\sigma = \frac{\partial g}{\partial \sigma}$.

Taking the expectation

$$\begin{aligned} E_t \left\{ F^{(1)}(y_{t-1}, u_t, \epsilon_{t+1}, \sigma) \right\} &= \\ & f(\bar{y}, \bar{y}, \bar{y}, 0) + f_{y_+} (g_y (g_y \hat{y} + g_u u + g_\sigma \sigma) + g_\sigma \sigma) \\ & + f_{y_0} (g_y \hat{y} + g_u u + g_\sigma \sigma) + f_{y_-} \hat{y} + f_u u \Big\} \\ &= (f_{y_+} g_y g_y + f_{y_0} g_y + f_{y_-}) \hat{y} + (f_{y_+} g_y g_u + f_{y_0} g_u + f_u) u \\ & + (f_{y_+} g_y g_\sigma + f_{y_0} g_\sigma) \sigma \\ &= 0 \end{aligned}$$

Recovering g_y

$$(f_{y+} g_y g_y + f_{y_0} g_y + f_{y-}) \hat{y} = 0$$

Structural state space representation:

$$\begin{bmatrix} 0 & f_{y+} \\ I & 0 \end{bmatrix} \begin{bmatrix} I \\ g_y \end{bmatrix} g_y \hat{y} = \begin{bmatrix} -f_{y-} & -f_{y_0} \\ 0 & I \end{bmatrix} \begin{bmatrix} I \\ g_y \end{bmatrix} \hat{y}$$

or

$$\begin{bmatrix} 0 & f_{y+} \\ I & 0 \end{bmatrix} \begin{bmatrix} y_t - \bar{y} \\ y_{t+1} - \bar{y} \end{bmatrix} = \begin{bmatrix} -f_{y-} & -f_{y_0} \\ 0 & I \end{bmatrix} \begin{bmatrix} y_{t-1} - \bar{y} \\ y_t - \bar{y} \end{bmatrix}$$

Structural state space representation

$$Dx_{t+1} = Ex_t$$

with

$$x_{t+1} = \begin{bmatrix} y_t - \bar{y} \\ y_{t+1} - \bar{y} \end{bmatrix} \quad x_t = \begin{bmatrix} y_{t-1} - \bar{y} \\ y_t - \bar{y} \end{bmatrix}$$

- There are multiple solutions but we want a unique stable one.
- Problem when D is singular.

Real generalized Schur decomposition

Taking the real generalized Schur decomposition of the pencil $\langle E, D \rangle$:

$$D = QTZ$$

$$E = QSZ$$

with T , upper triangular, S quasi-upper triangular, $Q'Q = I$ and $Z'Z = I$.

Generalized eigenvalues

λ_i solves

$$\lambda_i D x_i = E x_i$$

For diagonal blocks on S of dimension 1×1 :

- $T_{ii} \neq 0$: $\lambda_i = \frac{S_{ii}}{T_{ii}}$
- $T_{ii} = 0, S_{ii} > 0$: $\lambda_i = +\infty$
- $T_{ii} = 0, S_{ii} < 0$: $\lambda_i = -\infty$
- $T_{ii} = 0, S_{ii} = 0$: $\lambda_i \in \mathbb{C}$

A pair of complex eigenvalues

When a diagonal block of matrix S is a 2×2 matrix of the form

$$\begin{bmatrix} S_{ii} & S_{i,i+1} \\ S_{i+1,i} & S_{i+1,i+1} \end{bmatrix}:$$

- the corresponding block of matrix T is a diagonal matrix,
- $(S_{i,i} T_{i+1,i+1} + S_{i+1,i+1} T_{i,i})^2 < -4 S_{i+1,i} S_{i+1,i} T_{i,i} T_{i+1,i+1}$,
- there is a pair of conjugate complex eigenvalues

$$\lambda_i, \lambda_{i+1} =$$

$$\frac{S_{ii} T_{i+1,i+1} + S_{i+1,i+1} T_{i,i} \pm \sqrt{(S_{i,i} T_{i+1,i+1} - S_{i+1,i+1} T_{i,i})^2 + 4 S_{i+1,i} S_{i+1,i} T_{i,i} T_{i+1,i+1}}}{2 T_{i,i} T_{i+1,i+1}}$$

Applying the decomposition

$$\begin{aligned} D \begin{bmatrix} I \\ \textcolor{red}{g}_y \end{bmatrix} \textcolor{red}{g}_y \hat{y} &= E \begin{bmatrix} I \\ \textcolor{red}{g}_y \end{bmatrix} \hat{y} \\ \begin{bmatrix} T_{11} & T_{12} \\ 0 & T_{22} \end{bmatrix} \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} \begin{bmatrix} I \\ \textcolor{red}{g}_y \end{bmatrix} \textcolor{red}{g}_y \hat{y} \\ &= \begin{bmatrix} S_{11} & S_{12} \\ 0 & S_{22} \end{bmatrix} \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} \begin{bmatrix} I \\ \textcolor{red}{g}_y \end{bmatrix} \hat{y} \end{aligned}$$

where rows and columns are re-ordered such that:

- (T_{11}, S_{11}) contain stable generalized eigenvalues (modulus ≤ 1)
- (T_{22}, S_{22}) contain explosive generalized eigenvalues (modulus > 1)

Selecting the stable trajectory

To exclude explosive trajectories, one imposes

$$Z_{21} + Z_{22}g_y = 0$$

$$g_y = -Z_{22}^{-1}Z_{21}$$

A unique stable trajectory exists if Z_{22} is square and non-singular: there are as many roots larger than one in modulus as there are forward-looking variables in the model (Blanchard and Kahn condition) and the rank condition is satisfied.

An alternative algorithm: Cyclic reduction

- Solving

$$A_0 + A_1X + A_2X^2 = 0$$

- Iterate

$$A_0^{(k+1)} = -A_0^{(k)}(A_1^{(k)})^{-1}A_0^{(k)},$$

$$A_1^{(k+1)} = A_1^{(k)} - A_0^{(k)}(A_1^{(k)})^{-1}A_2^{(k)} - A_2^{(k)}(A_1^{(k)})^{-1}A_0^{(k)},$$

$$A_2^{(k+1)} = -A_2^{(k)}(A_1^{(k)})^{-1}A_2^{(k)},$$

$$\hat{A}_1^{(k+1)} = \hat{A}_1^{(k)} - A_2^{(k)}(A_1^{(k)})^{-1}A_0^{(k)}.$$

for $k = 1, \dots$ with $A_0^{(1)} = A_0$, $A_1^{(1)} = A_1$, $A_2^{(1)} = A_2$, $\hat{A}_1^{(1)} = A_1$ and
until $\|A_0^{(k)}\|_\infty < \epsilon$ and $\|A_2^{(k)}\|_\infty < \epsilon$.

- Then

$$X \approx -(\hat{A}_1^{(k+1)})^{-1}A_0$$

Recovering g_u

$$f_{y+} g_y g_u + f_{y_0} g_u + f_u = 0$$

$$g_u = -(f_{y+} g_y + f_{y_0})^{-1} f_u$$

Hong Lan & Alexander Meyer-Gohde, 2012. "[Existence and Uniqueness of Perturbation Solutions to DSGE Models](#)," SFB 649 Discussion Papers, Humboldt University, show that $f_{y+} g_y + f_{y_0}$ is an invertible matrix under standard regularity and saddle stability assumptions.

Recovering g_σ

$$f_{y+} g_y g_\sigma + f_{y_0} g_\sigma = 0$$

$$g_\sigma = 0$$

Yet another manifestation of the certainty equivalence property of first order approximation.

First order approximated decision function

$$y_t = \bar{y} + g_y \hat{y} + g_u u$$

$$\begin{aligned} E\{y_t\} &= \bar{y} \\ \Sigma_y &= g_y \Sigma_y g_y' + \sigma^2 g_u \Sigma_\epsilon g_u' \end{aligned}$$

The variance is solved for with an algorithm for Lyapunov equations.

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A simple RBC model

Consider the following model of an economy.

- Representative agent preferences

$$U = \sum_{t=1}^{\infty} \left(\frac{1}{1+\rho} \right)^{t-1} E_t \left[\log(C_t) - \frac{L_t^{1+\gamma}}{1+\gamma} \right].$$

The household supplies labor and rents capital to the corporate sector.

- ▶ L_t is labor services
- ▶ $\rho \in (0, \infty)$ is the rate of time preference
- ▶ $\gamma \in (0, \infty)$ is a labor supply parameter.
- ▶ C_t is consumption,
- ▶ w_t is the real wage,
- ▶ r_t is the real rental rate

RBC Model (continued)

- The household faces the sequence of budget constraints

$$K_t = K_{t-1}(1 - \delta) + w_t L_t + r_t K_{t-1} - C_t,$$

where

- ▶ K_t is capital at the end of period
- ▶ $\delta \in (0, 1)$ is the rate of depreciation
- The production function is given by the expression

$$Y_t = A_t K_{t-1}^\alpha ((1 + g)^t L_t)^{1-\alpha}$$

where $g \in (0, \infty)$ is the growth rate and α and β are parameters.

- A_t is a technology shock that follows the process

$$A_t = A_{t-1}^\lambda \exp(e_t),$$

where e_t is an i.i.d. zero mean normally distributed error with standard deviation σ_1 and $\lambda \in (0, 1)$ is a parameter.

The household problem

Lagrangian

$$L = \max_{C_t, L_t, K_t} \sum_{t=1}^{\infty} \left(\frac{1}{1+\rho} \right)^{t-1} E_t \left[\log(C_t) - \frac{L_t^{1+\gamma}}{1+\gamma} \right. \\ \left. - \mu_t (K_t - K_{t-1}(1-\delta) - w_t L_t - r_t K_{t-1} + C_t) \right]$$

First order conditions

$$\frac{\partial L}{\partial C_t} = \left(\frac{1}{1+\rho} \right)^{t-1} \left(\frac{1}{C_t} - \mu_t \right) = 0$$

$$\frac{\partial L}{\partial L_t} = \left(\frac{1}{1+\rho} \right)^{t-1} (L_t^\gamma - \mu_t w_t) = 0$$

$$\frac{\partial L}{\partial K_t} = - \left(\frac{1}{1+\rho} \right)^{t-1} \mu_t + \left(\frac{1}{1+\rho} \right)^t E_t (\mu_{t+1}(1-\delta + r_t)) = 0$$

First order conditions

Eliminating the Lagrange multiplier, one obtains

$$L_t^\gamma = \frac{w_t}{C_t}$$
$$\frac{1}{C_t} = \frac{1}{1+\rho} E_t \left(\frac{1}{C_{t+1}} (r_{t+1} + 1 - \delta) \right)$$

The firm problem

$$\max_{L_t, K_{t-1}} A_t K_{t-1}^\alpha \left((1+g)^t L_t \right)^{1-\alpha} - r_t K_{t-1} - w_t L_t$$

First order conditions:

$$r_t = \alpha A_t K_{t-1}^{\alpha-1} \left((1+g)^t L_t \right)^{1-\alpha}$$

$$w_t = (1-\alpha) A_t K_{t-1}^\alpha \left((1+g)^t \right)^{1-\alpha} L_t^{-\alpha}$$

Goods market equilibrium

$$K_t + C_t = K_{t-1}(1 - \delta) + A_t K_{t-1}^\alpha \left((1 + g)^t L_t \right)^{1-\alpha}$$

Dynamic Equilibrium

$$\frac{1}{C_t} = \frac{1}{1+\rho} E_t \left(\frac{1}{C_{t+1}} (r_{t+1} + 1 - \delta) \right)$$

$$L_t^\gamma = \frac{w_t}{C_t}$$

$$r_t = \alpha A_t K_{t-1}^{\alpha-1} ((1+g)^t L_t)^{1-\alpha}$$

$$w_t = (1-\alpha) A_t K_{t-1}^\alpha ((1+g)^t L_t)^{1-\alpha} L_t^{-\alpha}$$

$$K_t + C_t = K_{t-1}(1-\delta) + A_t K_{t-1}^\alpha ((1+g)^t L_t)^{1-\alpha}$$

Existence of a balanced growth path

There must exist a growth rates g_c and g_k so that

$$(1 + g_k)^t K_1 + (1 + g_c)^t C_1 = \frac{(1 + g_k)^t}{1 + g_k} K_1 (1 - \delta) + A \left(\frac{(1 + g_k)^t}{1 + g_k} K_1 \right)^\alpha ((1 + g)^t L_t)^{1-\alpha}$$

So,

$$g_c = g_k = g$$

Stationarized model

Let's define

$$\hat{C}_t = C_t / (1 + g)^t$$

$$\hat{K}_t = K_t / (1 + g)^t$$

$$\hat{w}_t = w_t / (1 + g)^t$$

Stationarized model (continued)

$$\frac{1}{\widehat{C}_t(1+g)^t} = \frac{1}{1+\rho} E_t \left(\frac{1}{\widehat{C}_{t+1}(1+g)(1+g)^t} (r_{t+1} + 1 - \delta) \right)$$

$$L_t^\gamma = \frac{\widehat{w}_t(1+g)^t}{\widehat{C}_t(1+g)^t}$$

$$r_t = \alpha A_t \left(\widehat{K}_{t-1} \frac{(1+g)^t}{1+g} \right)^{\alpha-1} ((1+g)^t L_t)^{1-\alpha}$$

$$\widehat{w}_t(1+g)^t = (1-\alpha) A_t \left(\widehat{K}_{t-1} \frac{(1+g)^t}{1+g} \right)^\alpha ((1+g)^t)^{1-\alpha} L_t^{-\alpha}$$

$$\begin{aligned} (\widehat{K}_t + \widehat{C}_t)(1+g)^t &= \widehat{K}_{t-1} \frac{(1+g)^t}{1+g} (1-\delta) \\ &\quad + A_t \left(\widehat{K}_{t-1} \frac{(1+g)^t}{1+g} \right)^\alpha ((1+g)^t L_t)^{1-\alpha} \end{aligned}$$

Stationarized model (continued)

$$\frac{1}{\widehat{C}_t} = \frac{1}{1+\rho} E_t \left(\frac{1}{\widehat{C}_{t+1}(1+g)} (r_{t+1} + 1 - \delta) \right)$$

$$L_t^\gamma = \frac{\widehat{w}_t}{\widehat{C}_t}$$

$$r_t = \alpha A_t \left(\frac{\widehat{K}_{t-1}}{1+g} \right)^{\alpha-1} L_t^{1-\alpha}$$

$$\widehat{w}_t = (1-\alpha) A_t \left(\frac{\widehat{K}_{t-1}}{1+g} \right)^\alpha L_t^{-\alpha}$$

$$\widehat{K}_t + \widehat{C}_t = \frac{\widehat{K}_{t-1}}{1+g} (1-\delta) + A_t \left(\frac{\widehat{K}_{t-1}}{1+g} \right)^\alpha L_t^{1-\alpha}$$

Dynare implementation

```
var C K L w r A;
```

```
varexo e;
```

```
parameters rho delta gamma alpha lambda g;
```

```
alpha = 0.33;
```

```
delta = 0.1;
```

```
rho = 0.03;
```

```
lambda = 0.97;
```

```
gamma = 0;
```

```
g = 0.015;
```

Dynare implementation (continued)

```
model;  
1/C=1/(1+rho)*(1/(C(+1)*(1+g)))*(r(+1)+1-delta);  
L^gamma = w/C;  
r = alpha*A*(K(-1)/(1+g))^(alpha-1)*L^(1-alpha);  
w = (1-alpha)*A*(K(-1)/(1+g))^alpha*L^(-alpha);  
K+C = (K(-1)/(1+g))*(1-delta)  
      +A*(K(-1)/(1+g))^alpha*L^(1-alpha);  
log(A) = lambda*log(A(-1))+e;  
end;
```

Dynare implementation (continued)

```
steady_state_model;  
A = 1;  
r = (1+g)*(1+rho)+delta-1;  
L = ((1-alpha)/(r/alpha-delta-g))*r/alpha;  
K = (1+g)*(r/alpha)^(1/(alpha-1))*L;  
C = (1-delta)*K/(1+g)  
    +(K/(1+g))^alpha*L^(1-alpha)-K;  
w = C;  
end;  
  
steady;
```

Dynare implementation (continued)

```
shocks;  
var e; stderr 0.01;  
end;  
  
check;  
  
stoch_simul(order=1);
```

Alternative implementation

Let Dynare detrend equations for you

```
parameters g;  
trend_var(growth_factor=1+g) Z; // Productivity trend  
var(deflator = Z) C K w;  
var L r A;  
varexo e;  
  
parameters rho delta gamma alpha lambda;  
  
model;  
// Declare non-detrended model equations  
end;
```

Decision and transition functions

Dynare output:

POLICY AND TRANSITION FUNCTIONS

	C	K	L	w	r	A
Constant	1.003043	3.125296	0.906526	1.003043	0.145450	1.000000
K(-1)	0.144433	0.779746	-0.105500	0.144433	-0.042523	0
A(-1)	0.757723	1.149948	0.589451	0.757723	0.204452	0.970000
e	0.781158	1.185514	0.607681	0.781158	0.210776	1.000000

$$C_t = 1.003 + 0.144 (K_{t-1} - \bar{K}) + 0.758 (A_{t-1} - \bar{A}) + 0.781e_t$$

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Dating variables in Dynare

Dynare will automatically recognize predetermined and non-predetermined variables, but you must observe a few rules:

- period t variables are set during period t on the basis of the state of the system at period $t - 1$ and shocks observed at the beginning of period t .
- therefore, stock variables must be on an end-of-period basis: investment of period t determines the capital stock at the end of period t .

Note: with the `predetermined_variables` command, one can use a beginning-of-period convention for stocks when writing the model. However, the IRFs and other output will still be at end-of-stock convention.

Log-linearization

- Taking a log-linear approximation of a model is equivalent to take a linear approximation of a model with respect to the logarithm of the variables.
- In practice, it is sufficient to replace all occurrences of variable X with $\exp(LX)$ where $LX = \log X$.
- It is possible to make the substitution for some variables and not others. You wouldn't want to take a log approximation of a variable whose steady state value is negative ...
- There is no evidence that log-linearization is more accurate than simple linearization. In a growth model, it is often more natural to do a log-linearization.

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The role of the Dynare preprocessor

- Dynare solves generic problems
- the preprocessor reads your *.mod file and translates it in specific MATLAB/Octave files
- *filename.m*: main MATLAB/Octave script for the model
- *filename_static.m*: static model
- *filename_dynamic.m*: dynamic model
- *filename_steadystate2.m*: steady state function
- *filename_set_auxiliary_variables.m*: auxiliary variables function

Overall design of Dynare

