

CIA model as in Walsh p112

The preference of the households is given by:

$$U = E \sum_{t=0}^{\infty} \beta^t \left[ \frac{c_t^{1-\Phi}}{1-\Phi} + \Psi \frac{(1-n_t)^{1-\eta}}{1-\eta} \right], \quad 0 < \beta < 1 \quad (1)$$

The CIA is given by:

$$c_t \leq \frac{m_{t-1}}{1+\pi_t} + \tau_t \quad (2)$$

The budget constraint takes the following form:

$$y_t + (1-\delta)k_{t-1} + \tau_t + \frac{m_{t-1} + (1+i_{t-1})b_{t-1}}{1+\pi_t} \geq c_t + k_t + m_t + b_t \quad (3)$$

Aggregate output,  $y_t$  is given by the following production function:

$$y_t = e^{z_t} k_{t-1}^\alpha n_t^{1-\alpha} \quad (4)$$

The technology shock follows an AR(1) process and is given by:

$$z_t = \rho z_{t-1} + \xi_t \quad (5)$$

The rate of growth of money is equal to  $m_t = \frac{(1+\theta_t)}{1+\pi_t} m_{t-1}$

The FOC are

$$c_t : \quad c_t^{-\Phi} = \lambda_{1t} + \lambda_{2t} \quad (6)$$

$$n_t : \quad \Psi(1-n_t)^{-\eta} = (1-\alpha)\lambda_{2t} \frac{y_t}{n_t} \quad (7)$$

$$k_t : \quad \lambda_{2t} = \beta E_t \left[ \lambda_{2t+1} \left( \alpha \frac{y_{t+1}}{k_t} + (1-\delta) \right) \right] \quad (8)$$

$$m_t : \quad \lambda_{2t} = \beta E_t \left( \frac{\lambda_{1t+1} + \lambda_{2t+1}}{1+\pi_{t+1}} \right) \quad (9)$$

$$b_t : \quad \lambda_{2t} = \beta E_t \lambda_{2t+1} \left( \frac{1+i_t}{1+\pi_{t+1}} \right) \quad (10)$$

$$\lambda_{1t} : \quad c_t = \frac{m_{t-1}}{1+\pi_t} + \tau_t \quad (11)$$

$$\lambda_{2t} : \quad c_t + k_t + m_t + b_t = y_t + (1-\delta)k_{t-1} + \frac{m_{t-1} + (1+i_{t-1})b_{t-1}}{1+\pi_t} + \tau_t \quad (12)$$

My Dynare equations are:

$$\Psi(1-n_t)^{-\eta} = E_t \left[ \frac{(1-\alpha)\beta}{1+\pi_{t+1}} \right] c_{t+1}^{-\Phi} \left( \frac{y_t}{n_t} \right) \quad (13)$$

$$E_t \left[ \frac{\beta}{1+\pi_{t+1}} \right] c_{t+1}^{-\Phi} = E_t \left[ \frac{\beta^2}{1+\pi_{t+2}} \right] c_{t+2}^{-\Phi} \left[ \frac{\alpha y_{t+1}}{k_t} + (1-\delta) \right] \quad (14)$$

$$y_t = c_t + i_t \quad (15)$$

$$k_t = i_t + (1-\delta)k_{t-1} \quad (16)$$

$$y_t = e^{z_t} k_{t-1}^\alpha n_t^{1-\alpha} \quad (17)$$

$$w_t = (1 - \alpha) \frac{y_t}{n_t} \quad (18)$$

$$r_t = (1 - \alpha) \frac{y_t}{k_{t-1}} \quad (19)$$

$$1 + r_t = \frac{1 + i_t}{1 + \pi_t} \quad (20)$$

$$z_t = \rho_1 z_{t-1} + e1_t \quad (21)$$

$$m_t = \left( \frac{1 + \theta_t}{1 + \pi_t} \right) m_{t-1} \quad (22)$$

$$\theta_t = \rho_2 \theta_{t-1} + \rho_3 z_{t-1} + e2_t \quad (23)$$